

Example Item 3A.1a

Primary Target 3A (Content Domain G), Secondary Target 1I (CCSS 8.G.C), Tertiary Target 3F

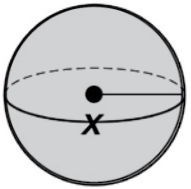
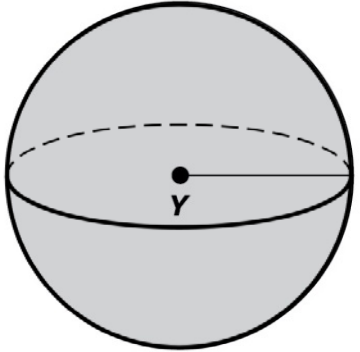
The radius of sphere Y is twice the radius of sphere X. A student claims that the volume of sphere Y must be exactly twice the volume of sphere X.

Part A:

Drag numbers into the boxes to create one example to evaluate the student’s claim.

Part B:

Decide whether the student’s claim is True, False, or whether it Cannot be determined. Select the correct option.

0 1 2 3 4 5 6 7 8 9	<p>Part A:</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>Radius = <input type="text"/> in</p> <p>Volume = $\frac{4}{3} \pi$ <input type="text"/> in³</p> </div> <div style="text-align: center;">  <p>Radius = <input type="text"/> in</p> <p>Volume = $\frac{4}{3} \pi$ <input type="text"/> in³</p> </div> </div>	
	<p>Part B:</p> <p style="text-align: center;"> <input type="radio"/> True <input type="radio"/> False <input type="radio"/> Cannot be determined </p>	

Rubric: (1 point) The student supplies an example of two radii and missing numbers for the volumes that makes the conjecture false (e.g., radiuses are 1 and 2, missing numbers are 1 and 8; radii are 2 and 4, missing numbers are 8 and 64; radiuses are 1.5 and 3, missing numbers are 3.375 and 27; etc.) and responds with “False” in part B.

Response Type: Drag and Drop

Example Item 3A.1b

Primary Target 3A (Content Domain F-IF), Secondary Target 1K (CCSS F-IF.A)

The equation of a circle in the coordinate plane with center (0, 0) and radius 5 is shown:

$$x^2 + y^2 = 25$$

Fill in the table to show an example of two ordered pairs that show this equation does **not** define y as a function of x .

x	y

Rubric: (1 point) The student enters the coordinates of two points that have the same x -coordinates and different y -coordinates and that lie on the circle in the response box ($-5 \leq x \leq 5$ and $y = \pm\sqrt{25 - x^2}$).

Response Type: Fill-in Table

Example Item 3A.1c

Primary Target 3A (Content Domain N-RN), Secondary Target 1B (CCSS N-RN.3), Tertiary Target 3D

Consider the two numbers a and b as well as their sum and product.

Drag values for a and b into the boxes to make the paired statements true for both $a \cdot b$ and $a + b$.

If none of the values make both statements true, leave the boxes empty for that pair of statements.

	Statements	Example
3		
5	$a \cdot b$ is an irrational number	$a =$ <input type="text"/>
$\sqrt{3}$	$a + b$ is a rational number	$b =$ <input type="text"/>
$\sqrt{5}$	$a \cdot b$ is a rational number	$a =$ <input type="text"/>
$3\sqrt{5}$	$a + b$ is an irrational number	$b =$ <input type="text"/>
$5 - \sqrt{3}$	$a \cdot b$ is an irrational number	$a =$ <input type="text"/>
	$a + b$ is an irrational number	$b =$ <input type="text"/>

Rubric: (1 point) The student drags correct combinations of values that result in the indicated rational and irrational perimeters and areas of the rectangle. (e.g., see one possible solution at right). Other correct responses are possible.

Response Type: Drag and Drop

Statements	Example
$a \cdot b$ is an irrational number $a + b$ is a rational number	$a =$ <input type="text" value="√3"/> $b =$ <input type="text" value="5 - √3"/>
$a \cdot b$ is a rational number $a + b$ is an irrational number	$a =$ <input type="text" value="√5"/> $b =$ <input type="text" value="3√5"/>
$a \cdot b$ is an irrational number $a + b$ is an irrational number	$a =$ <input type="text" value="√5"/> $b =$ <input type="text" value="√3"/>

Example Item 3A.1d

Primary Target 3A (Content Domain G-CO), Secondary Target 1X (CCSS G-CO.9), Tertiary Target 3G

A geometry student made this claim:

If any two lines are cut by a transversal, then alternate interior angles are always congruent.

Part A:

Draw a diagram that shows two lines cut by a transversal with alternate interior angles that **are** congruent **or** select **None** if there is not a situation that supports the student's claim.

Part A:

None

Part B:

Draw a diagram that shows two lines cut by a transversal with alternate interior angles that are **not** congruent **or** select **None** if the student's claim is always true.

Part B:

None

Rubric: (1 point) The student draws a transversal through two parallel lines to create congruent alternate interior angles in Part A and through two non-parallel lines for Part B.

Response Type: Graphing and Hot Spot

Target 3B: Construct, autonomously, chains of reasoning that will justify or refute propositions or conjectures.

General Task Model Expectations for Target 3B

- Items for this target should focus on the core mathematical work that students are doing around the real number system, algebra, functions, and geometry.
- Items for this target can require students to solve a multi-step, well-posed problem involving the application of mathematics to a real-world context. The difference between items for Claim 2A and Claim 3B is that the focus in 3B is on communicating the reasoning process in addition to getting the correct answer.
- Many machine-scorable items for these task models can be adapted to increase the autonomy of student’s reasoning process but would require hand-scoring.

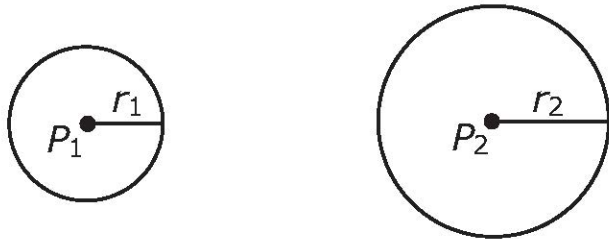
Task Model 3B.1

- The student is presented with a proposition or conjecture. The student is asked to identify or construct reasoning that justifies or refutes the proposition or conjecture.
- Items in this task model often address more generalized reasoning about a class of problems or reasoning that generalizes beyond the given problem context even when it is presented in a particular case.

Example Item 3B.1a

Primary Target 3B (Content Domain G-C), Secondary Target 1X (CCSS G-C.A), Tertiary Target 3?

Proposition. All circles are similar.



The four statements below can be completed and ordered to outline an argument that proves this proposition.

1.	Translate Circle [drop-down choices: 1, 2] from [drop-down choices: P_1, P_2] to [drop-down choices: P_1, P_2] so that the two circles have the same center.
2.	Dilate Circle [drop-down choices: 1, 2] with center [drop-down choices: P_1, P_2] by a factor of [drop-down choices: $r_1, r_2, r_1/r_2, r_2/r_1$].
3.	The circles now coincide, showing they are similar.
4.	Given Circle 1 with center P_1 and radius r_1 and Circle 2 with center P_2 and radius r_2 .

Rubric: (2 points) The student completes and orders the four statements that support the claim in a logical order (Examples below. Note that the order of 2 and 3 can be reversed but 1 must be first and 4 must be last. Also note that the ordering of 2 and 3 changes the correct center of dilation).

(1 point) The student completes and orders the four statements that support the claim in a logical order but either chooses some of the options from the drop-down menus incorrectly or chooses them in a sensible way if the order were correct, but the order is not correct.

High School Claim 3 Specifications

Example 1

1. Given Circle 1 with center P_1 and radius r_1 and Circle 2 with center P_2 and radius r_2 .
2. Translate Circle 2 from P_2 to P_1 so that the two circles have the same center.
3. Dilate Circle 2 with center P_1 by a factor of r_1/r_2 .
4. The circles now coincide, showing they are similar.

Example 2

1. Given Circle 1 with center P_1 and radius r_1 and Circle 2 with center P_2 and radius r_2 .
2. Dilate Circle 1 with center P_1 by a factor of r_2/r_1 .
3. Translate Circle 1 from P_1 to P_2 so that the two circles have the same center.
4. The circles now coincide, showing they are similar.

Response Type: Drag and Drop, Drop-down Menu⁷

⁷ Drop-Down Menu response type is not yet available in the Smarter Balanced item authoring tool, but it is a scheduled enhancement by 2017.

High School Claim 3 Specifications

Example Item 3B.1b

Primary Target 3B (Content Domain A-APR), Secondary Target 1? (CCSS A-APR.A), Tertiary Target 3?

Kiera claimed that the sum of two linear polynomials with rational coefficients is always a linear polynomial with rational coefficients.

Drag the six statements into a logical sequence to outline an argument that proves this claim.

1.	$p(x) + q(x) = (ax+cx) + (b+d)$
2.	$p(x) + q(x) = (ax+b) + (cx+d)$
3.	Given $p(x) = ax+b$ and $q(x) = cx+d$ where $a, b, c,$ and d are rational numbers.
4.	$(a+c)$ and $(b+d)$ are rational numbers
5.	So $p(x) + q(x)$ is a linear polynomial with rational coefficients.
6.	$p(x) + q(x) = (a+c)x + (b+d)$

Rubric: (2 points) The student completes and orders the four statements that support the claim in a logical order (Example below. Note that 1 must come first, 6 must come last, the order of 2, 3, and 4 must be preserved but 5 can go anywhere in between 1 and 6).

(1 point) The student completes and orders the four statements that support the claim in a logical order but either chooses some of the options from the drop-down menus incorrectly or chooses them in a sensible way if the order were correct, but the order is not correct.

Example

1. Given $p(x) = ax+b$ and $q(x) = cx+d$ where $a, b, c,$ and d are rational numbers.
2. $p(x) + q(x) = (ax+b) + (cx+d)$
3. $p(x) + q(x) = (ax+cx) + (b+d)$
4. $p(x) + q(x) = (a+c)x + (b+d)$
5. $(a+c)$ and $(b+d)$ are rational numbers
6. So $p(x) + q(x)$ is a linear polynomial with rational coefficients.

Response Type: Drag and Drop

Example Item 3B.1c

Primary Target 3B (Content Domain F-TF), Secondary Target 1? (CCSS F-TF.C), Tertiary Target 3?

Suppose θ is an acute angle. Then $\sin^2(\theta) + \cos^2(\theta) = 1$.

Drag the six statements into a logical sequence to outline an argument that proves this claim.

1.	Construct a right triangle that includes θ as one of its acute angles.
2.	So $\sin^2(\theta) + \cos^2(\theta) = 1$.
3.	Give the label a to the side that is adjacent to θ , the label b to the side that is opposite θ , and the label c to the hypotenuse.
4.	$\frac{a^2}{c^2} + \frac{b^2}{c^2} = 1$ if we divide both sides by c^2 .
5.	$a^2 + b^2 = c^2$ by the Pythagorean Theorem.
6.	$\sin(\theta) = \frac{b}{c}$ and $\cos(\theta) = \frac{a}{c}$ by the definition of $\sin(\theta)$ and $\cos(\theta)$.

Rubric: (1 point) The student completes and orders the four statements that support the claim in a logical order (example below. Note that 1 and 2 must come first, 5 and 6 must come last, but the order of 3 and 4 can be switched).

Example

1. Construct a right triangle that includes θ as one of its acute angles.
2. Label the side adjacent to θ a , the side opposite θ b , and the hypotenuse c .
3. $\sin(\theta) = b/c$ and $\cos(\theta) = a/c$ by the definition of $\sin(\theta)$ and $\cos(\theta)$.
4. $a^2 + b^2 = c^2$ by the Pythagorean Theorem.
5. $a^2/c^2 + b^2/c^2 = 1$ if we divide both sides by c^2 .
6. So $\sin^2(\theta) + \cos^2(\theta) = 1$.

Response Type: Drag and Drop

Task Model 3B.2

- The student is asked a mathematical question and is asked to identify or construct reasoning that justifies his or her answer.
- Items in this task model often address more generalized reasoning about a class of problems or reasoning that generalizes beyond the given problem context even when it is presented in a particular case.

Example Item 3B.2a

Primary Target 3B (Content Domain A-APR), Secondary Target 1F (CCSS A-APR.B)

$P(x)$ is a 4th degree polynomial. The graph of $y = P(x)$ has exactly three distinct x -intercepts. Which polynomial could be $P(x)$?

- A. $x^3(x-3)$
- B. $x^2(x-2)(x-1)$
- C. $(x-3)(x-2)(x-1)$
- D. $x(x-3)(x-2)(x-1)$

For **one** of the polynomials above, explain why it could **not** be $P(x)$.

The graph of $y =$ [drop-down choices: the four polynomials listed in the table] has exactly [drop-down choices: 0, 1, 2, 3, 4] distinct x -intercepts at

$x =$ [0] [1] [2] [3] [4]

Click on all of the distinct x -intercepts

The degree of this polynomial is [drop-down choices: 0, 1, 2, 3, 4].

Rubric: (2 points) The student clicks on the correct polynomial (B) and selects one of the polynomials, identifies the correct number of distinct x -intercepts, correctly identifies the x -intercepts, and correctly identifies the degree of the polynomial. (See Example below. This is just one possibility.)

(1 point) The student clicks on the polynomials that could be $P(x)$ or fills out the information about one of the polynomials correctly.

High School Claim 3 Specifications

Example:

The graph of $y = x^3(x-3)$ has exactly 2 distinct x -intercepts at

- $x = [0] [1] [2] [3] [4]$

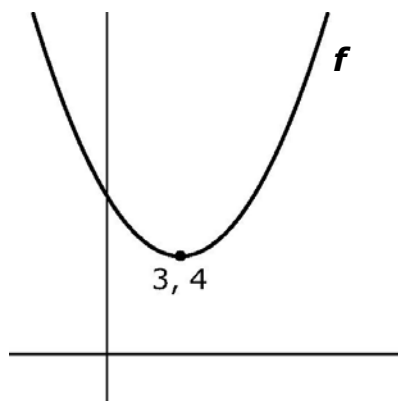
The degree of this polynomial is 4.

Response Type: Multiple Choice, single correct response and Drop Down Menu

Example Item 3B.2b

Primary Target 3B (Content Domain F-BF), Secondary Target 1N (CCSS F-BF.B), Tertiary Target 3E

The graph of a quadratic function f is shown and the vertex is labeled with its coordinates.
If $g(x) = f(x-1)+2$, what is the minimum value of g ?



The minimum value of g is $[1, 2, 3, 4, 5, 6]$ because the minimum value for f is $[1, 2, 3, 4, 5, 6]$ and the graph of g is shifted $[up, down, left, right]$ from the graph of f by $[1, 2, 3, 4, 5, 6]$ units (in addition to the other shift).

Rubric: (1 points) The student selects the correct choices from the drop-down menus (6; 4; up; 2 or 6; 4; right; 1).

Response Type: Drop Down Menu

Note: The functionality for this item does not currently exist, but it could be implemented as a multiple choice or hotspot currently. Drop down choices are given in the brackets.

Example Item 3B.2c

Primary Target 3B (Content Domain F-IF), Secondary Target 1L (CCSS F-IF.B), Tertiary Target 3F

A student examines two graphs representing the functions $f(x) = x + 5$ and $g(x) = x^2 + 5$. The student notices that the graphs both have a y -intercept at the point $(0, 5)$. The student makes the following claim:

"For any real number c , the y -intercepts for the graphs of $y = c \cdot f(x)$ and $y = c \cdot g(x)$ are the same."

Is this true or false?

If it is **true**, enter the y -coordinate of the y -intercept in terms of c . $(0, [\quad])$

If it is **false**, enter the y -coordinates of the y -intercepts of the two graphs that are a counter-example. $(0, [\quad])$; $(0, [\quad])$

Rubric: (1 point) The student is able to identify the correct y -coordinate of the y -intercept and enter it into the first response box ($5c$).

Response Type: Equation/Numeric

Task Model 3B.3

- Items for this target require students to solve a multi-step, well-posed problem involving the application of mathematics to a real-world context.
- The difference between Claim 2 task models and this task model is that the student needs to provide some evidence of his/her reasoning. The difference between Claim 4 task models and this task model is that the problem is completely well posed and no extraneous information is given.

High School Claim 3 Specifications

Example Item 3B.3a

Primary Target 3B (Content Domain N-Q), Secondary Target 1C (CCSS N-Q.A), Tertiary Target 4F

- 1 hour = 60 minutes
- 1 kilometer = 100 meters
- 1 mile \approx 1.6 kilometers

Calvin biked 24 miles in 2 hours. What is his approximate average speed in meters per minute?

Explain or show clear steps for how you determined your answer.

Rubric: (2 points) The student enters the correct numeric value in the response (32) and enters a coherent, complete explanation or sequence of computations that shows where this comes from (see Examples).

(1 point) The student enters the correct numeric value in the response but does not provide a coherent explanation OR the student enters a different number in the response but includes an explanation that shows an understanding of how the answer could be found, but with some computational errors or a small misstep in reasoning.

Example 1

24 miles in 2 hours is 12 mi/hr.

$12 \text{ mi/hr} * 60 \text{ min/hr} = 1/5 \text{ mi/min.}$

1 km is 100 meters and 1 mile is 1.6 km, so 1 mile is 160 meters.

$1/5 \text{ mi/min} * 160 \text{ m/mi} = 32 \text{ meters per minute.}$

Example 2

Going 24 miles in 2 hours is the same as going 12 miles per hour.

There are 100 meters in a km and 1.6 km in a mile, so there are 160 m in a mile. There are 60 minutes in an hour.

1 mile per hour is 160 meters per 60 minutes which is $8/3$ meters per minute, so

12 miles per hour is $12 * 8/3 = 32$ meters per minute.

Response Type: Short Text (handscored)

Target 3C: State logical assumptions being used.**General Task Model Expectations for Target 3C**

- Items for this target should focus on the core mathematical work that students are doing around the real number system, algebra, functions, and geometry.
- For some items, the student must explicitly identify assumptions that
 - Make a problem well-posed, or
 - Make a particular solution method viable.
- When possible, items in this target should focus on assumptions that are commonly made implicitly and can cause confusion when left implicit.
- For some items, the student will be given a definition and be asked to reason from that definition.

Task Model 3C.1

- The student is asked to identify an unstated assumption that would make the problem well-posed or allow them to solve a problem using a given method.

Example Item 3C.1

Primary Target 3C (Content Domain A-REI), Secondary Target 1H, Tertiary Target 3G

Beth is solving this equation: $\frac{1}{x} + 3 = \frac{3}{x}$.

She says "I can multiply both sides by x and get the linear equation $1 + 3x = 3$, whose solution is $x = \frac{2}{3}$."

Which of the following statements makes this a correct argument, or shows that it is incorrect? Select **all** that apply.

- A. You can assume $x \neq 0$ because both sides are undefined if $x = 0$.
- B. After multiplying both sides by x you need to subtract 1 from both sides.
- C. You cannot multiply both sides by x because you do not know what x is.
- D. The equation is not linear, so you cannot use the methods normally used for solving linear equations.

Rubric: (1 point) The students selects A, or A and B.

Response type: Multiple Choice, multiple correct response

High School Claim 3 Specifications

Task Model 3C.2

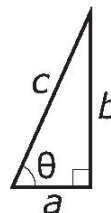
- The student will be given one or more definitions or assumptions and will be asked to reason from that set of definitions and assumptions.

Example Item 3C.2a

Primary Target 3C (Content Domain F-TF), Secondary Target 10 (CCSS G-SRT.C)

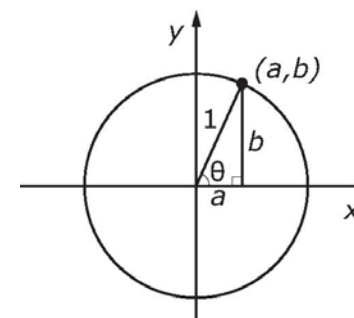
For an acute angle θ , $\sin(\theta)$ can be defined in terms of the side-lengths of a right triangle that includes angle θ . Here is the definition:

Given a right-triangle with side-lengths a and b and hypotenuse c , if θ is the angle opposite b , then $\sin(\theta) = \frac{b}{c}$.



Part A:

In the figure, angle θ has a vertex at the origin, its initial side corresponds to the positive x -axis, and the terminal side intersects the unit circle at the point (a, b) .

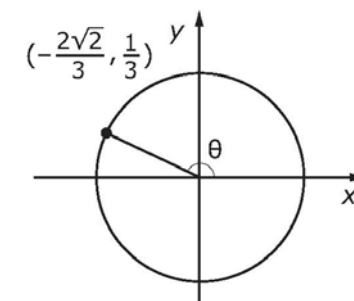


What is $\sin(\theta)$ in terms of a and b according to the definition given? Enter your answer in the first response box.

Part B:

For angles that are not acute, the definition of $\sin(\theta)$ is given in terms of the unit circle.

If angle θ has a vertex at the origin, its initial side corresponds to the positive x -axis, and the terminal side intersects the unit circle at the point (a, b) , then $\sin(\theta) = b$.



In the figure shown, what is $\sin(\theta)$? Enter your answer in the second response box.

Rubric: (1 point) The student enters the correct value for $\sin(\theta)$ according to the given definition (b ; $1/3$).

Response type: Equation/Numeric

Note: It would be best to implement this so students answer Part A before they go on to Part B, once this functionality is installed. They should still be able to go back and change their answer to Part A.

Example Item 3C.2b

Primary Target 3B (Content Domain A-APR), Secondary Target 1X (CCSS A-APR.A)

Proposition 1 The sum of two linear polynomials with integer coefficients is always a linear polynomial with integer coefficients.

The Closure of the Integers Under Addition The sum of two integers is always an integer

The Commutative Property If A and B are real numbers, then $A + B = B + A$

The Associative Property If A , B , and C are real numbers, then $(A + B) + C = A + (A + C)$

The Distributive Property If A , B , and C are real numbers, then $A(B + C) = AB + AC$

The Any-Order Property of Addition The sum of two or more real numbers can be performed in any order or any grouping.

The outline of a proof of Proposition 1 is shown. Add one or more justifications for steps 3, 4, and 5 of the proof.

Statement	Justification
1. Given $p(x) = ax+b$ and $q(x) = cx+d$ where a , b , c , and d are integers.	Hypothesis
2. $p(x) + q(x) = (ax+b) + (cx+d)$	By Definition
3. $p(x) + q(x) = (ax+cx) + (b+d)$	
4. $p(x) + q(x) = (a+c)x + (b+d)$	
5. $(a+c)$ and $(b+d)$ are integers	
6. So $p(x) + q(x)$ is a linear polynomial with integer coefficients.	Conclusion

Rubric: (1 point) The student provides a correct justification for each step of the proof (Example below. Note that for step (3), students can either cite the any-order property of addition or cite the commutative and associative properties together).

High School Claim 3 Specifications

Example

Statement	Justification
1. Given $p(x) = ax+b$ and $q(x) = cx+d$ where $a, b, c,$ and d are integers.	Hypothesis
2. $p(x) + q(x) = (ax+b) + (cx+d)$	By Definition
3. $p(x) + q(x) = (ax+cx) + (b+d)$	The Any-Order Property of Addition
4. $p(x) + q(x) = (a+c)x + (b+d)$	The Distributive Property
5. $(a+c)$ and $(b+d)$ are integers	The Closure of the Integers Under Addition
6. So $p(x) + q(x)$ is a linear polynomial with rational coefficients.	Conclusion

Response Type: Drag and Drop

Example Item 3C.2c

Primary Target 3C (Content Domain A-APR), Secondary Target 1F (CCSS A-APR.C), Tertiary Target 3B

An **algebraic identity** is an equation that is always true for any value of the variables.

For example, $2(x+y) = 2x+2y$ is an identity because of the distributive property.

For each equation, select "Yes" if the equation is an algebraic identity. Select "No" if it is not an algebraic identity.

Equation	Yes	No
$(x+3)^2 = x^2 + 3^2$		
$y^{-1} = \frac{1}{y}$ if $y \neq 0$		
$a^2 + b^2 = c^2$		

Rubric: (1 point) The student correctly indicates which equation is an identity and which is not (NYN).

Response Type: Matching Table

Target 3D: Use the technique of breaking an argument into cases.**General Task Model Expectations for Target 3D**

- Items for this target should focus on the core mathematical work that students are doing around the real number system, algebra, functions, and geometry.
- The student is given
 - A problem that has a finite number of possible solutions, some of which work and some of which don't, or
 - A proposition that is true in some cases but not others.
- Items for Claim 3 Target D should either present an exhaustive set of cases to consider or expect students to consider all possible cases in turn in order to distinguish it from items in other targets.

Task Model 3D.1

- The student is given a problem that has a finite number of possible solutions that need to be treated on a case-by-case basis.

Example Item 3D.1a

Primary Target 3D (Content Domain F-IF), Secondary Target 1M (CCSS F-IF.C).

Consider the piecewise-defined function given by

$$f(x) = \begin{cases} 2x - 7 & \text{for } x < -1 \\ x^2 + 3 & \text{for } -1 \leq x < 3 \\ x - 1 & \text{for } x \geq 3 \end{cases}$$

For how many real values of x does $f(x)=0$?

- A. 0
- B. 1
- C. 2
- D. 3

Rubric: (1 point) The student selects the correct number of zeros for the function (A).

Response Type: Multiple Choice, single correct response

Commentary: This could be implemented with an equation/numeric response type. By varying the functions defining each piece, you can cover a wide variety of content from the Functions domain.

Example Item 3D.1b

Primary Target 3D (Content Domain F-BF), Secondary Target 1N (CCSS F-BF.A), Tertiary Target 3C

An arithmetic sequence is a sequence in which the difference between any two consecutive terms is the same. For example, the sequence 2, 9, 16, 23, 30, 37 is an arithmetic sequence because the difference between any two consecutive numbers is 7.

Suppose that an arithmetic sequence of integers starts with a 5 and also later includes an 11.

5, ...?.... , 11, _____

Which number could **not** be the term that immediately follows 11 in the sequence?

- A. 12
- B. 13
- C. 14
- D. 15
- E. 17

Rubric: (1 point) The student selects the number that could not be the next term in an arithmetic sequence (D).

Response Type: Multiple Choice, single correct response

High School Claim 3 Specifications

Task Model 3D.2

- The student is given a proposition and asked to determine in which cases the proposition is true.

Example Item 3D.2a

Primary Target 3D (Content Domain A-SSE), Secondary Target 1D (CCSS A-SSE.A)

Mrs. Beno wrote this equation on the board and asked, "Is this a true equation?"

$$(x+y)^2 = x^2+y^2$$

Nigel said, "Sometimes it is, and sometimes it isn't."

For each case shown, determine whether this equation is true or false.

Case	True	False
$x \neq 0, y \neq 0$		
$x = 0, y \neq 0$		
$x \neq 0, y = 0$		
$x = 0, y = 0$		

Rubric: (1 point) The student correctly indicates which conditions make the equation true and which make it false (FTTT).

Response Type: Matching Table

Example Item 3D.2b:

Primary Target 3D (Content Domain N-RN), Secondary Target 3G, Tertiary Target 1X (CCSS N-RN.1),

Consider this inequality: $\sqrt[3]{m} \leq m$

Part A:

Determine the positive values of m for which the inequality is **true**.
Enter your response as an inequality in the first response box.

Part B:

Determine the positive values of m for which the inequality is **false**.
Enter your response as an inequality in the second response box.

High School Claim 3 Specifications

Rubric: (2 points) The student provides the values that make the given inequality true ($m \geq 1$) and false ($0 < m < 1$). (1 point) The student errors in the use of the inequality signs (uses $>$ instead of \geq or \leq instead of $<$) but otherwise has the correct range of values. OR The student is able to provide an example of where the statement is true (e.g., a positive value greater than or equal to 1) and a number between 0 and 1 that makes the statement false.

Response Type: Equation/Numeric

Example Item 3D.2c:

Primary Target 3D (Content Domain A-REI), Secondary Target 3G, Tertiary Target 1X (CCSS A-REI.A),

Determine whether each statement is

- true for all values of x ,
- true for some values of x , or
- not true for any value of x

Statement	True for all	True for some	Not true for any
If $x^2 = 9$, then $\sqrt{9} = x$			
If $x^3 = y$, then $\sqrt[3]{y} = x$			
If $(-x)^4 = y$, then $\sqrt[4]{y} = (-x)$			

Rubric: (1 point) The student correctly selects True for all, True for some, or Not true for any for each statement correctly (see below).

Statement	True for all	True for some	Not true for any
If $x^2 = 9$, then $\sqrt{9} = x$			
If $x^3 = y$, then $\sqrt[3]{y} = x$			
If $(-x)^4 = y$, then $\sqrt[4]{y} = (-x)$			

Response Type: Matching Tables

Target 3E: Distinguish correct reasoning from flawed reasoning

General Task Model Expectations for Target 3E

- Items for this target should focus on the core mathematical work that students are doing around the real number system, algebra, functions, and geometry.
- The student is presented with valid or invalid reasoning and told it is flawed or asked to determine its validity. If the reasoning is flawed, the student identifies, explains, and/or corrects the error or flaw.
- The error should be more than just a computational error or an error in counting, and should reflect an actual error in reasoning.
- Analyzing faulty algorithms is acceptable so long as the algorithm is internally consistent and it isn't just a mechanical mistake executing a standard algorithm.

Task Model 3E.1

- Some flawed reasoning or student work is presented and the student identifies and/or corrects the error or flaw.
- The student is presented with valid or invalid reasoning and asked to determine its validity. If the reasoning is flawed, the student will explain or correct the flaw.

Example Item 3E.1a

Primary Target 3E (Content Domain A-REI), Secondary Target 1H (CCSS A-REI.A)

A student solves a quadratic equation this way:

Equation: $x^2 - 3x - 4 = 0$

Step 1: $x^2 - 3x = 4$

Step 2: $x(x - 3) = 4$

Step 3: $x = 2$ or $x - 3 = 2$

Step 4: $x = 2$ or $x = 5$

The solution is incorrect. Identify the step that does not follow logically from the previous step.

- A. Step 1
- B. Step 2
- C. Step 3
- D. Step 4

Rubric: (1 point) Student selects the incorrect step (C).

Response Type: Multiple Choice, single correct response

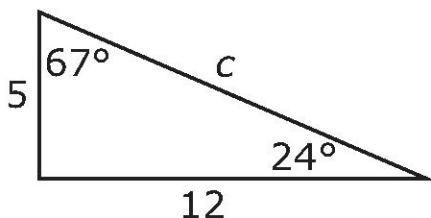
Commentary: Step 1 is a distractor because although it is procedurally unproductive, it does follow logically from the previous step. A variation on this task could ask the student say whether or not the solution is correct.

Example Item 3E.1b

Primary Target 3E (Content Domain Geometry) Secondary Target 1X (CCSS 8.G.B)

Brandon uses the following reasoning to find the length c of the third side in the triangle shown.

“The two legs of the triangle are 5 and 12. I know by the Pythagorean Theorem that $5^2 + 12^2 = c^2$. I calculate $5^2 + 12^2 = 25 + 144 = 169$. My calculator says that the square root of 169 is 13, so $c = 13$.”



Which statement is true about this reasoning?

- A. Brandon’s reasoning is correct.
- B. The Pythagorean Theorem does not apply to this triangle.
- C. The Pythagorean Theorem applies, but Brandon made a calculation error.
- D. It is true that $c = 13$, but Brandon’s reasoning is incorrect because he used a calculator.

Rubric: (1 point) Student selects the correct answer (B).

Response Type: Multiple Choice, single correct response

Task Model 3E.2

- Two or more approaches or chains of reasoning are given and the student is asked to identify the correct method and justification OR identify the incorrect method/reasoning and the justification.

Example Item 3E.2a

Primary Target 3E (Content Domain N-Q), Secondary Target 1C (CCSS N-Q.A), Tertiary Target Grade 7 1A

<p>Sherry wants to enlarge a photograph to 300% of its original size. The machine she is using can only make enlargements for the following percentages: 100%, 125%, 150%, and 200%.</p> <p>Sherry thinks that she should enlarge the photograph by 100% and then by 200% to get a total enlargement of 300%.</p> <p>Decide if Sherry is correct. If Sherry is correct, drag the 100 and 200 from the palette into the first two answer spaces.</p> <p>If Sherry is incorrect, drag a sequence of enlargements she can use to get a total enlargement of 300%.</p> <p>Each enlargement percentage may be used more than once. If a sequence is not needed, leave the box blank.</p>	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 10%; text-align: center;">%</th> <th style="text-align: center;">Sequence of Enlargements</th> </tr> </thead> <tbody> <tr> <td style="text-align: center;">100</td> <td style="text-align: center;">1: <input style="width: 50px;" type="text"/> %</td> </tr> <tr> <td style="text-align: center;">125</td> <td style="text-align: center;">2: <input style="width: 50px;" type="text"/> %</td> </tr> <tr> <td style="text-align: center;">150</td> <td style="text-align: center;">3: <input style="width: 50px;" type="text"/> %</td> </tr> <tr> <td style="text-align: center;">150</td> <td style="text-align: center;">4: <input style="width: 50px;" type="text"/> %</td> </tr> <tr> <td style="text-align: center;">200</td> <td style="text-align: center;">5: <input style="width: 50px;" type="text"/> %</td> </tr> </tbody> </table>	%	Sequence of Enlargements	100	1: <input style="width: 50px;" type="text"/> %	125	2: <input style="width: 50px;" type="text"/> %	150	3: <input style="width: 50px;" type="text"/> %	150	4: <input style="width: 50px;" type="text"/> %	200	5: <input style="width: 50px;" type="text"/> %
%	Sequence of Enlargements												
100	1: <input style="width: 50px;" type="text"/> %												
125	2: <input style="width: 50px;" type="text"/> %												
150	3: <input style="width: 50px;" type="text"/> %												
150	4: <input style="width: 50px;" type="text"/> %												
200	5: <input style="width: 50px;" type="text"/> %												

Rubric: The student drags the percentages into the appropriate boxes to show Sherry is incorrect (e.g., 200, 150. Other correct responses are possible).

Response Type: Drag and Drop

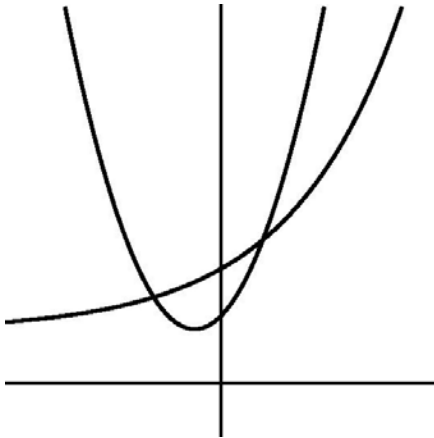
Target 3F: Base arguments on concrete referents such as objects, drawings, diagrams, and actions**Task Model 3F.1**

- The student uses concrete referents to help justify or refute an argument.

Example Item 3F.1a

Primary Target 3F (Content Domain A-REI), Secondary Target 1J (CCSS A-REI.D), Tertiary Target 3B

The two graphs shown represent the equations $y = P \cdot b^x$ and $y = a(x-h)^2 + k$, where $a, b > 0$, and h, k , and P are rational numbers.



Which statement best describes the number of solutions the equation $P \cdot b^x = a(x-h)^2 + k$ has and why?

- A. There is only one solution because b can't be negative.
- B. There are no solutions to this equation because you can't solve it.
- C. There are exactly two solutions because the graphs intersect twice.
- D. There could be three solutions because the graphs might intersect at a third point.

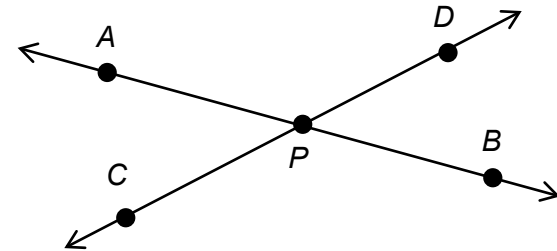
Rubric: (1 point) Student selects the correct answer (D).

Response type: Multiple Choice, single correct response.

Example Item 3F.1b

Primary Target 3F (Content Domain G-CO), Secondary Target 10 (CCSS G-CO.C), Tertiary Target 3B

The line through A and B intersects the line through C and D at point P , as shown in the figure. Prove that angle APC is congruent to angle BPD .



Rubric: (2 points) The student gives a correct argument for the angle congruence (see Examples).

(1 point) The student gives a response that shows some understanding of a correct argument, but some details are missing or unclear.

Example 1

Since A and B lie on a line, a 180 degree rotation about point P will take ray PA to ray PB and vice versa.

Similarly, since C and D lie on a line, a 180 degree rotation about point P will take ray PC to ray PD and vice versa.

Thus a 180 degree rotation about point P will take angle APC to angle BPD , showing they are congruent.

Example 2

Angles APB and CPD are both 180 degrees.

So $(\text{measure angle } CPA) + (\text{measure angle } APD) = 180$ and

$(\text{measure angle } APD) = 180 - (\text{measure angle } CPA)$.

Also, $(\text{measure angle } APD) + (\text{measure angle } DPB) = 180$.

Substituting for angle APD in the third equation, we get

$180 - (\text{measure angle } CPA) + (\text{measure angle } DPB) = 180$.

Subtracting the first two numbers in the left from both sides of the equation shows

$(\text{measure angle } DPB) + (\text{measure angle } CPA)$.

If two angles have equal measures, they are congruent.

Response Type: Short text (handscored)

Target 3G: Determine conditions under which an argument does and does not apply

Target 3G is a closely related extension of the expectations in Targets 3A, 3B, 3C, and 3D, and as with those targets, is often a tertiary alignment for items in those targets. Students often test propositions and conjectures with specific examples (as described in Target 3A) for the purpose of formulating conjectures about the conditions under which an argument does and does not apply. Students then must explicitly describe those conditions (as in Target 3C). Expectations for Target 3D include determining conditions under which an argument is true given cases—the next step is articulating those cases autonomously.